SPLINE FINITE DIFFERENCE METHOD FOR A CLASS OF BOUNDARY-VALUE PROBLEMS

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 ${\bf Abstract.}\ \ {\rm In\ this\ paper,\ we\ consider\ spline\ finite\ difference\ method\ based\ on\ uniform\ mesh\ for\ solving\ a\ class\ of\ two-point\ boundary\ value\ problems\ of\ the\ form$

$$e^{-\alpha x}(e^{\alpha x}u')' = f(x, u), a \le x \le b,$$

$$u(a) = A, u(b) = B$$

is presented. Three-point finite difference method using splines is obtained for the solution. We show that the resulting method provides second order convergence. Two test examples are solved to demonstrate the efficiency of the method.

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Received 13-06-2007, Accepted 14-05-2008. $2000\ Mathematics\ Subject\ Classification:$ 65L10, CR:G1.7

Key words and Phrases: Two-point boundary value problems, finite difference methods, spline solution, continuity condition.

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