A SMALL ANGLE NEUTRON SCATTERING STUDY OF PHASE SEPARATION KINETICS IN ITS EARLY STAGES IN Cu-0.9 AT% Ti

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ABSTRACT

ASMALL ANGLE NEUTRON SCATTERING STUDY OF PHASE SEPARATION KINETICS IN ITS EARLY STAGES IN Cu-0.9 at% Ti. Phase separation kinetics in supersaturated Cu-0.9at% Ti alloys after isothermal heat treatment at 300°C (573 K) are investigated by small and wide angle neutron scattering. A fine scale dispersion of the second phase Cu₄Ti within a copper-titanium solid solution, which is accumulated during the very early stage of phase separation, can lead to significant strengthening. Up to the present, no investigation has covered these very early stages in copper titanium alloys. The low titanium content of 0.9 at% was chosen in order to have a better possibility to study the phase separation process in its early stages. The chosen low aging temperature leads to slow decomposition kinetics and, hence, is favourable to investigate early stage decomposition. Small angle neutron scattering (SANS) is used in this work because of its ability to provide access to structural analysis of unmixing alloys, in both the early stages where the composition fluctuation can be small in spatial extension and in amplitude, and in the later stages of decomposition. These later stages are needed to be covered, in order to assess the transition from earlier stages to the later stages of phase separation.

Key words: Cu-0.9at% Ti alloys, phase separation, early stages, SANS

INTRODUCTION

An addition of a few percent titanium to the copper matrix is well known to enhance its strength substantially, which is rendered possible by both solid solution and, in particular, age hardening. Without any
addition of other metallic elements, pure copper is a good conductor and can easily be plastically formed at room temperature, but it suffers from a lack of strength. A fine scale dispersion of second phase precipitates within the matrix of a copper-titanium alloy can lead to significant strengthening. This commonly results from the decomposition of the solid solution during cooling from the single phase state at high temperature into the two-phase state at lower temperatures. For reasons of entropy, the single phase state \( \alpha \) of a solid solution with a certain composition is thermodynamically stable only at elevated temperature. At lower temperatures the free energy of a binary system is lowered through phase separation or decomposition of \( \alpha \) phase into two phases \( \alpha' \) and \( \beta \).

One of the interesting and attractive properties of highly supersaturated Cu-Ti alloys develop from the formation of periodic precipitate microstructures during aging, giving rise to satellites around the main Bragg’s Peaks [1]. Those Cu-Ti alloys thus belong to a class of alloys, which are termed “sidebands” alloys.

Decomposition of supersaturated metastable solid solutions is initiated via formation of stable nuclei of the second phase, then proceeds to a more or less pronounced growth regime, and finally ends in a coarsening reaction of the precipitates. In the ‘classical’ picture of decomposition of a metastable supersaturated solution, during nucleation and growth of stable nuclei the matrix becomes depleted from solute atoms. This leads to an increase for the critical size \( R' \) of the nuclei, and consequently results in a strong decrease of nucleation rate. The coarsening reaction starts when the supersaturation of the matrix has been reduced so much that the critical radius \( R' \) becomes larger than the radii \( R \) of the smaller precipitates within the size distribution. The latter then start to redissolve [2 – 4].

**EXPERIMENTAL**

**Preparation of Samples**

According to copper titanium phase diagram mentioned above, a low titanium concentration of 0.9 at% Ti and a low aging temperature of 300 °C are chosen, in order to assure the alloy to lie within the two phase region below the metastable coherent solvus line for Cu-0.9at% Ti and to make sure that the reaction kinetics are rather sluggish. Therefore, these slow-motion processes in phase separation kinetics during the early stages of the decomposition reaction can be followed experimentally.

The single crystal samples of Cu-0.9at% Ti necessary for this present study, were grown by the Bridgman technique, in which a mold containing the melt, is lowered from the hot zone of a vertical tubular furnace into the cold zone. In order to initiate a precipitation reaction, the alloy is first homogenized in the single phase region and then quenched into brine prior to isothermal aging at a temperature within the two phase region. The homogenization temperatures used are 750 °C and 850 °C, under a dried Argon atmosphere, and after this homogenization the single crystals are rapidly quenched into water. A salt bath and a vacuum furnace are used for a short and a long aging time respectively.

Many Cu-Ti samples had been homogenized at 750 °C; 850 °C, and then step by step aged at 300 °C for different aging times. Samples number 15 and 19 represent the two homogenization temperatures, namely sample 15 at 850 °C, and sample 19 at 750 °C. Aging times for these two Cu-Ti samples are shown in Table 1.

**Table 1. Aging treatments at 300 °C of samples 15 and 19**

<table>
<thead>
<tr>
<th>Sample 15</th>
<th>Sample 19</th>
</tr>
</thead>
<tbody>
<tr>
<td>Homogenized</td>
<td>Aged [s]</td>
</tr>
<tr>
<td>850 °C</td>
<td>20</td>
</tr>
<tr>
<td>60</td>
<td>1</td>
</tr>
<tr>
<td>120</td>
<td>2</td>
</tr>
<tr>
<td>300</td>
<td>5</td>
</tr>
<tr>
<td>600</td>
<td>10</td>
</tr>
<tr>
<td>1200</td>
<td>20</td>
</tr>
<tr>
<td>3600</td>
<td>60</td>
</tr>
<tr>
<td>7200</td>
<td>120</td>
</tr>
<tr>
<td>18 x 10^3</td>
<td>300</td>
</tr>
<tr>
<td>36 x 10^3</td>
<td>600</td>
</tr>
<tr>
<td>486 x 10^3</td>
<td>8100</td>
</tr>
</tbody>
</table>

**Optimization of the Aging Temperature**

As the objective of the present work is to study unmixing of the low alloyed Cu-0.9at% Ti during the early stages, the aging temperature must be optimized such that diffusion of Ti atoms in the Cu-matrix is still possible, i.e. the aging temperature \( T_A \) must be sufficiently
high. On the other hand, $T_A$ must be sufficiently low for the unmixing kinetics to be kept sufficiently slow.

For this purpose we chose $T_A = 300 \, ^\circ \text{C}$ (573 K) for following reason: The diffusion length, $x_{\text{diff}}$, covered by a diffusing Ti atom ought to be larger than the mean distance, $x_{\text{nuc}}$, between two Cu$_x$Ti nuclei. $x_{\text{diff}}$ can be estimated from the chemical diffusion coefficient as

$$D_{t_f} = D_0 \cdot e^{-Q/RT} \quad \text{(1)}$$

It was measured for a Cu-0.9 at% Ti solid solution between 973 K and 1283 K [5]. It has been given as

$$D_{t_f}(T) = 1.4 \times 10^{-4} \cdot \exp\left(-\frac{2044 \cdot 10^3}{R \cdot T}\right) \left[\frac{\text{m}^2}{\text{s}}\right] \quad \text{(2)}$$

where $Q$ is the activation enthalpy, $R$ the molar gas constant. The diffusion coefficients $D_{t_f}$ could not be measured at temperatures below 973 K. Thus, in order to estimate $D_{t_f}$ at 573 K, one has to extrapolate the high temperature data which Eq. (2) is based on, to low temperatures. For 573 K one obtains

$$D_{t_f}(573 \, \text{K}) = 3.54 \times 10^{-23} \left[\frac{\text{m}^2}{\text{s}}\right] \quad \text{(3)}$$

$x_{\text{diff}}$ after aging time of $t_A$ at $300 \, ^\circ \text{C}$ is estimated from

$$x_{\text{diff}} = \frac{1}{D_{t_f}(573 \, \text{K}) \cdot t_A} \quad \text{(4)}$$

As we are interested in early stage decomposition reactions, $x_{\text{diff}}$ after an aging time of $t_A = 20 \, \text{s}$ at $300 \, ^\circ \text{C}$ can be accounted for by substitution of $D_{t_f}$ from Eq. (3) into Eq. (4). One obtains

$$x_{\text{diff}} = 2.6 \times 10^{-7} \text{m} = 260 \, \text{nm}$$

The average interparticle distance can be estimated from a relation $x_{\text{nuc}} \approx \frac{1}{\sqrt{N_v}}$, if one assumes that Cu$_x$Ti particles to be arranged on cubic lattice with lattice constant $x_{\text{nuc}}$, can be estimated from :

$$N_v = \frac{f_e}{\frac{4 \pi}{3} \cdot R_{LSW}^3} \quad \text{(5a)}$$

and

$$f_e = \frac{c_{x} - c_e}{c_p - c_e} \quad \text{(5b)}$$

Here $f_e$ denotes the equilibrium precipitated volume fraction $f_e \equiv f(t_A \rightarrow \infty)$ which will be attained after long aging times once the nucleation process has terminated. $R_{LSW}$ represents the size of the critical nuclei, and may be given as [6]

$$R_{LSW} = \frac{2 \sigma_{\text{aff}} \cdot V_n}{R \cdot T} \cdot \frac{1 - c_e}{c_p - c_e} \cdot \frac{1}{\ln \frac{c_0}{c_e}} \quad \text{(6)}$$

with : $\sigma_{\text{aff}}$ = interfacial energy between Cu matrix and Cu$_x$Ti particle = 0.031 J/m$^2$ [7]

$c_o$ = the nominal Ti concentration, which in this case is 0.9 at%

$c_p$ = the Ti content in the Cu$_x$Ti particles, in this case 20 at%

$c_e$ = concentration of Ti in solid solution with the fully precipitated Cu$_x$Ti microstructure

$V_n = 7.8 \, \text{cm}^3/\text{mol}$ is the molar volume of Cu$_x$Ti particle

From Eq. (6) one obtains

$$R_{LSW}(t_A \rightarrow 0) = 0.79 \, \text{nm}$$

which is in a good agreement with the experimental results.

If one now assumes that at the earliest stage of unmixing, the precipitated volume fraction,

$$f(t \rightarrow 0) \approx \frac{1}{10} \cdot f_e(t \rightarrow \infty)$$

one finally obtains from Eqs. (5) and (6) :

$$x_{\text{nuc}} = \frac{1}{\sqrt{N_v}} = \left[\frac{4 \pi}{3} \cdot R_{LSW}^3 \cdot f_e\right]^{1/3} = R_{LSW} \left[\frac{4 \pi}{3} \cdot \frac{10(c_p - c_e)}{c_0 - c_e}\right]^{1/3} \, \text{nm}$$

This estimation clearly shows that

$$x_{\text{diff}} \gg x_{\text{nuc}}$$

and thus indicating that the mobility of Ti atoms in the Cu matrix is sufficient to migrate during $20 \, \text{s}$ at $300 \, ^\circ \text{C}$ over distances which correspond to more than the separation length between two nuclei.

One therefore may infer that one can follow the precipitation reaction in Cu-0.9 at% Ti during isothermal aging at $300 \, ^\circ \text{C}$ within a time window ranging from a few seconds to some hours. Hence, an aging temperature of $300 \, ^\circ \text{C}$ seems to be appropriate for studying the early stage decomposition kinetics in a Cu-0.9 at% Ti alloy.

**SANS Measurement of Cu-0.9 at% Ti Samples**

The Cu-0.9 at% Ti sample is first measured in its homogenized condition in order to get a reference scattering curve before the phase separation has occurred. This data would be used as a standard for the analysis of scattering curves after the samples being aged and measured. The difference in SANS-curve taken from aged and homogenized samples contains actually the information on the aging process, or in other words, the information on the state of separation in the particular sample. These informations come from interparticle interference of the scattered wave.
SANS-2 facility at Geesthacht Neutron Facility (GeNF) in GKSS Research Centre (Geesthacht-Germany) was used for this work. SANS-2 is one of the two SANS beam lines at GeNF. The neutrons produced in the nuclear reactor FRG-1 and cooled down in the cold source are guided through neutron guide No. 8 to this instrument. A sketch of the SANS-2 set-up is shown in Fig. 2.

Velocity selector with $\Delta \lambda/\lambda$ of 10 % (standard) and 20 % resolution are used as monochromators. Wavelengths of 0.4 and 0.57 nm were used during the measurements. Two Cu-0.9at% Ti single crystal samples were chosen to show the phase separation kinetics process in these alloys, and in addition for wide angle measurement (WANS) with the 2nd detector, a pure copper sample was used as a reference. This copper sample was measured together with the Cu-Ti samples in each step during measurements, in order to assure the acceptable conditions of the neutron flux during experiments. Measured intensity was corrected for sample transmissions, background, and detector efficiency. The absolute cross-sections were calculated by comparison with the incoherent scattering from vanadium.

**DATA REDUCTION AND DATA ANALYSIS**

Since a great deal of the theory of neutron scattering involves the calculation of the differential cross-sections, the data reduction and data analyses must also be related to the differential cross-sections.

The terms of data reduction and data analyses, technically refer to different procedures. Data reduction refers to procedures such as background subtraction, whereas data analyses refers to procedures of data interpretation, fitting theoretical models to the experimental scattering curves, etc.

A set of software programs for viewing, reducing, and analysing SANS data which have been written by colleagues from GKSS Research Centre Geestacht were used for this work.

One of the program mentioned above is SANDRA (as an abbreviation of SANS Data Reduction and Analyses), which is used to view SANS spectra and calculating scattering curves by radial or sector integration of the spectra.

SANDRA calculates the macroscopic differential cross-sections from the recorded experimental data as follows

$$\frac{d\Sigma}{d\Omega}(\kappa) = \frac{I(\Omega)}{M \cdot \left(\frac{f(\lambda)}{M}\right) \Delta\Omega \eta T_r L} \quad \text{................. (7)}$$

where:

- $M$ = monitor for the neutron count rate after monochromator
- $\eta$ = detector efficiency
- $T_r$ = sample transmission

**Table 2. Time-dependent parameters of the Cu$_4$Ti precipitate microstructure**

<table>
<thead>
<tr>
<th>Sample 19</th>
<th>$t_A/300 \degree$C</th>
<th>$\dot{C} \times 10^3$</th>
<th>$f(t) \times 10^2$</th>
<th>$R$ [nm]</th>
<th>$N_c(t) \times 10^{23}$ [cm$^{-3}$]</th>
</tr>
</thead>
<tbody>
<tr>
<td>00 s</td>
<td>8.76</td>
<td>Not determ.</td>
<td>Not determ.</td>
<td>0.36</td>
<td>2.75</td>
</tr>
<tr>
<td>20 s</td>
<td>8.36</td>
<td>0.26</td>
<td>0.38</td>
<td>0.36</td>
<td>2.75</td>
</tr>
<tr>
<td>60 s</td>
<td>8.32</td>
<td>0.28</td>
<td>0.39</td>
<td>0.38</td>
<td>2.75</td>
</tr>
<tr>
<td>300 s</td>
<td>7.92</td>
<td>0.44</td>
<td>0.40</td>
<td>0.40</td>
<td>2.75</td>
</tr>
<tr>
<td>3600 s</td>
<td>6.49</td>
<td>1.03</td>
<td>0.57</td>
<td>2.75</td>
<td>2.75</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Sample 15</th>
<th>$t_A/300 \degree$C</th>
<th>$\dot{C} \times 10^3$</th>
<th>$f(t) \times 10^2$</th>
<th>$R$ [nm]</th>
<th>$N_c(t) \times 10^{23}$ [cm$^{-3}$]</th>
</tr>
</thead>
<tbody>
<tr>
<td>00 s</td>
<td>8.75</td>
<td>Not determ.</td>
<td>Not determ.</td>
<td>0.36</td>
<td>2.75</td>
</tr>
<tr>
<td>20 s</td>
<td>8.36</td>
<td>0.26</td>
<td>0.38</td>
<td>0.36</td>
<td>2.75</td>
</tr>
<tr>
<td>60 s</td>
<td>8.32</td>
<td>0.28</td>
<td>0.39</td>
<td>0.38</td>
<td>2.75</td>
</tr>
<tr>
<td>120 s</td>
<td>8.29</td>
<td>0.29</td>
<td>0.39</td>
<td>0.39</td>
<td>2.75</td>
</tr>
<tr>
<td>300 s</td>
<td>7.92</td>
<td>0.44</td>
<td>0.40</td>
<td>0.40</td>
<td>2.75</td>
</tr>
<tr>
<td>1200 s</td>
<td>7.64</td>
<td>0.56</td>
<td>0.43</td>
<td>0.43</td>
<td>2.75</td>
</tr>
<tr>
<td>3600 s</td>
<td>6.95</td>
<td>0.84</td>
<td>0.46</td>
<td>0.46</td>
<td>2.75</td>
</tr>
<tr>
<td>7200 s</td>
<td>6.12</td>
<td>1.17</td>
<td>0.48</td>
<td>0.48</td>
<td>2.75</td>
</tr>
<tr>
<td>18.10 s</td>
<td>4.08</td>
<td>1.69</td>
<td>0.52</td>
<td>0.52</td>
<td>2.75</td>
</tr>
<tr>
<td>36.10 s</td>
<td>2.79</td>
<td>2.51</td>
<td>0.63</td>
<td>0.63</td>
<td>2.75</td>
</tr>
<tr>
<td>486.10 s</td>
<td>2.01</td>
<td>2.82</td>
<td>1.47</td>
<td>1.47</td>
<td>2.75</td>
</tr>
</tbody>
</table>
Since the incident neutron count rate in front of the sample \( I_0 \) could not be measured right at that position where the incident neutron beam enters the sample, it was necessary to use a relation with the neutron count rate \( M \), from a detector which was positioned behind the monochromator (c.f. Figure 2). After reducing the measured data from its background and other corrections needed, one receives a corrected curve which then is ready for further interpretation.

The calculated time-dependent values of \( f(t_A) \) for both samples 15 and 19 are shown in a Table 2.

**RESULTS AND DISCUSSIONS**

Figures 3 and 4 show the two dimension spectra of sample 15. These four of 2d-SANS pattern of \(<100>\) oriented single crystal clearly show an anisotropic scattering intensity maxima along the \(<001>\) and \(<010>\) directions. The anisotropy pointing towards strong alignment of the longer c-axis of the tetragonally distorted \( \text{Cu}_4\text{Ti} \) particles into \(<100>\) directions, increases during longer aging times of sample 15, starting from its homogeneous condition (Figure 3) to the longest aging times of 135 h (8100 min) at 300°C (Figure 4).

**Figure 3.** Sample 15: Homogenized at 750 °C and quenched

**Figure 4.** Sample 15: Aging for 8100 min at 300 °C

**Figure 5.** Scattering curves for sample 19 in different aging states; both SANS data and WANS data were used for obtaining the shown scattering curves
Figure 5 shows the scattering curves of sample 19 for five different states of heat-treatment. Even in its homogenized condition, it can be clearly recognized that very small precipitates had been formed already during quenching, i.e., the state of a homogeneous solid solution could not be sustained upon quenching; the finely dispersed precipitation become discernible by a weak broad maximum in the cross-section of the dark-blue (homogenized) curve. SANS allows one to distinguish between different states of precipitate microstructures even if the sample has been aged for only 20 s at 300 °C following quenching. This clearly indicates that diffusion and associated unmixing is rather fast. Those differences in the scattering behaviour of a sample aged for 20 s are only disclosed by SANS but not WANS. However, the potential and benefit of employing also WANS show up in samples which had been aged at 300 °C at considerably longer aging times (e.g., t_A ≥ 5 min; Figure 6). Figure 6 shows the differences of Laue scattering (κ ≥ 6 nm⁻¹) as determined by WANS of sample 19, in comparison to the longest aging times, 8100 min (135 h), of sample 15, and a pure copper sample. From the rather similar Laue scattering of the long aged (135 h / 300 °C) sample 15 and the pure copper sample, one may infer most of the titanium atoms in the Cu-0.9 at% Ti alloy had already been consumed for the nucleation process and for further growth of the Cu₄Ti particles; only a few Ti atoms are left in solid solution.

CONCLUSIONS

The present study shows that a supersaturated Cu-0.9at% Ti had already undergone some unmixing during quenching, thus a homogeneous solid solution could not be established at the beginning of isothermal aging at 300 °C. However, nevertheless during short term aging at 300 °C the supersaturation was still sufficiently high to drive further unmixing. As the kinetics at 300 °C are rather sluggish, it became possible to follow the phase separation process experimentally in the early stages where nucleation still has occurred, by using small angle neutron scattering techniques (SANS). SANS provided the kinetic parameters to determine the time evolution of the precipitate volume fraction, the cluster size distribution and, hence, the cluster number density, and the mean cluster size, in fact, during the early stages of decomposition prior to significant coarsening. The scattering pattern clearly proved the precipitates to be of the metastable coherent type Cu₄Ti. The large coherency strains associated with the high number density of Cu₄Ti particles will give rise to an efficient and strong strengthening of the two phase Cu-Ti alloy.

As the present work has yielded quantitative insight into time evolution of the precipitate microstructure and, on particular, the time evolution of the mean size and the number density of the Cu₄Ti particles, all relevant parameters for following the strengthening potential of the precipitate microstructure at different aging stages have been obtained. It is thus recommended to correlate the evolution of the precipitate microstructure with its influence on age hardening. For this purpose, single crystals with the same composition and aging treatments should be subjected to a study of their yield strength or hardness.

REFERENCES


