29

Students Algebraic Thinking Processes in Mathematics Problem Solving at Low Mathematic Ability Student Based on Quantitative Reasoning Ability

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Abstract. *Quantitative Reasoning* is students ability on conclused a problem solved. The purpose of this research has information about algebraic thinking processed on student with low ability based on *Quantitative Reasoning* ability. Methods used qualitative descriptive with purpose for desription about algebraic thinking processed on mathematic problem solving basic material on function with low ability of student based on quantitative reasoning ability. This paper used algebraic ability paper tes and interview transcript. Subject cluster used *purposive technic* with apretiation high value on raport and teacher review which known about students characteristic. The results showed that algebraic thinking processed on mathematic problem solving on student with low ability based on quantitative reasoning ability obtained Less category because subject didn't capable used deductive reasoning on clarify *n* symbol on problem solved and representation on arrow diagram and cartesius diagram for the first test. That result showed *Quantitative Reasoning* subject on analyzed problems to extract and quantify essential features with deductive reasoning on conclude highest bounce of the ball from the graph and function table. That result showed *Quantitative Reasoning* subject on analyzed problems to extract and quantify essential features with inductive reasoning subject on analyzed problems to extract and function table. That result showed *Quantitative Reasoning* subject on analyzed problems to extract and quantify essential features with inductive reasoning subject on analyzed problems to extract and quantify essential features with inductive reasoning subject on analyzed problems to extract and quantify essential features with inductive reasoning obtained "Less" category.

Keywords: algebraic thinking processed, function material, low mathematic ability, *quantitative reasoning* ability.

Abstrak. Quantitative Reasoning merupakan kemampuan siswa dalam menyimpulkan suatu permasalahan. Tujuan dari penelitian ini adalah untuk mengetahui lebih mendalam mengenai proses berpikir aljabar terutama pada siswa dengan kemampuan rendah ditinjau dari kemampuan Quantitative Reasoning. Metode penelitian adalah deskriptif kualitatif dengan tujuan untuk mendeskripsikan proses berpikir aljabar siswa dalam penyelesaian masalah matematika materi fungsi pada siswa kemampuan rendah ditinjau dari kemampuan quantitative reasoning. Instrumen dalam penelitian ini adalah lembar tes kemampuan berpikir aljabar dan lembar wawancara. Pemilihan subjek dilakukan secara purposive dengan mempertimbangkan nilai rapor tertinggi dan pertimbangan guru kelas yang lebih mengetahui karakteristik siswa. Hasil penelitian menunjukkan bahwa proses berpikir aljabar dalam penyelesaian masalah matematika siswa kemampuan rendah ditinjau dari kemampuan quantitative reasoning memperoleh kategori kurang karena subjek belum mampu menggunakan penalaran deduktif dalam menjelaskan makna simbol n dalam permasalahan dan merepresentasikan dalam diagram panah dan diagram cartesius pada soal nomor satu sehingga memperoleh kategori kurang. Subjek juga belum mampu menggunakan penalaran induktif dalam menyimpulkan lambungan tertinggi bola berdasarkan tabel fungsi yang diperjelas dengan grafik fungsi pada soal nomor dua.

Kata kunci: proses berpikir aljabar, fungsi, kemampuan matematika rendah, kemampuan *quantitative reasoning*.

INTRODUCTION

Education is human effort to develop appropriate personality with culture and points on daily activities to be able encounter every changed because of advancement science and technology existence (Habibi, Darhim, Turmudi, 2018). Sumardyono (2004: 28) clarified objective on mathematics education emphasized on student was skill for capable applicable mathematics to mathematical problem solving, other study or another problem which is related with daily activities. It is show that important skill for student elaboration is problem solving ability.

Problem solving ability could has support student to development and solved about mathematics problem which is appeared on daily activities or mathematical problem on other knowledge level. Problem solving stages applied in this research was Polya problem solving stages. These stages included : 1) understanding the problem, 2) devising a plan, 3) carry out a plan 4) looking back the conclusion (2004: 5). Polya problem solving stages application on learning process expected to students could have solved about problem which is constitute development of previous example accord applied working out proprietary problem on accord student ability.

In most of the daily activities we have found some aspects of algebraic thinking. Ameron (2002: 4) clarified algebraic thinking was mental processes like reasoning with unknowns, generalizing and formalizing relations between magnitudes and developing the concept variable') and algebraic symbolizing (symbol manipulation on paper). Algebraic thinking according by Herbert and Brown (1997:123) is using mathematical symbols and tools to analyze different situations by 1) extracting information from a situation, 2) representing that information mathematically in words, diagrams, tables, graphs, and equations, 3) interpreting and applying functional relationships to the same situation and to new related situation. According to the Kieran (2004: 142) Algebraic thinking could be interpreted as an approach to quantitative situations that emphasizes the general relational aspects with tools that are not necessarily letter-symbolic but which can ultimately be used as cognitive support for introducing and for sustaining the more traditional discourse of school algebra.

Some of definition showed with algebraic thinking students carry out an activities on effort analyze, representation, and make generalizing to symbols, pattern's and numbers which is represented by words, tables, images, diagrams and mathematics expressions. According to Berg (2009: 275) on title research "*Developing Algebraic Thinking In A Community Of Inquiry*" showed that participants research development of algebraic thinking were deeply interwoven with the processes related to the creation and development of the community of inquiry. Algebraic thinking has some component include algebra as mathematical thinking tools such as problem solving skills, representation skills, and *quantitative reasoning* skills, and algebra as fundamental algebraic ideas such as generalized arithmetic, the language of mathematics, and a tool for functions and mathematical modelling. Beside that, almost of students have problems on algebraic thinking processed on functional materials such as 1) arithmetic operation working out problems, 2) interpreted and understood symbols problem, 3) representation the situation as functional graphs problem. Properly, students must acquire both competencies that is problem solved ability and algebraic thinking ability in order to has full algebraic thinking understanding.

Reasoning is thinking processed on conclusion withdraw processed (Sumarno, 2013: 148). It has two kind are inductive reasoning and deductive reasoning. Conclusion withdraw based on some problem or limited pattern of problems is unductive reasoning. Beside that conclusion withdraw

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31

based on unanimously rules is deductive reasoning. Quantitative reasoning on mathematic is ability which is capable development on mathematic learning to analyze quantitative information and determine problem solving and procedure could be applied on certain problem to obtain a conclusion. Quantitative reasoning for basicly or objective value focused on problem solving. It is include six ability : 1) read and comprehenly information on many patterns, 2) interpretation quantitative information and make representation for conclusion, 3) used arithmetic problem solving, algebra, geometry, and statistic method, 4) estimate the answer and investigate advisability, 5) communicate quantitative information, and 6) make a definition from mathematic or statistic method.

Quantitative reasoning on algebra according Kaput & Blanton (2005: 99) were "Algebraic reasoning is a process in which students generalize mathematical ideas from a set of particular instances, establish those generalizations through the discourse of argumentation, and express them in increasingly formal and age-appropriate ways". Quantitative reasoning on algebra emphasized conclusion withdraw based on datas or quantitative information. This reasoning was important because is the greatest way to solved many type for problem solving. Quantitative reasoning on algebra could help students to understood and development concepts on algebra representation, analyzed problems to extract and quantify essential features on deductive or inductive reasoning.

Based on background, researcher was interest to arranged research with title "Students Algebraic Thinking Processed In Mathematic Problem Solving At Low Mathematic Ability Student Based On Quantitative Reasoning Ability". This research aim to aims to analyze algebraic thinking processed in mathematic problem solving by low mathematic ability based on *quantitative reasoning* ability.

RESEARCH METHODS

This research was conducted by using qualitative approach with descriptive method. The subjects of this research were three students who has high mathematic ability, intermediate mathematic ability, and low mathematic ability that was chosen by purposive sampling technique on three category from mathematic raport and teacher reviews which know more about students characteristic. They were from SMP Plus Rahmat Kediri. The source for this research was algebraic thinking test result with compability from the indicator sheet and direct interview with questionnaire. From subject, researcher could analysed and identify to presented in the form of a algebraic thinking description. Algebraic thinking processed were elaborated to be three indicator, such as explain in the Table Caption 1.

No.	Component	Indicator					
1.	Problem Solving	Using problem solving strategies.					
	Skills	Exploring multiple approaches or multiple solutions.					
2.	Representation Skills	Displaying relationships, visually, symbolically, numerically,					
		verbally.					
		Translating among different representations.					
		Interpreting information within representations.					
		Representing mathematical ideas using equations, tables,					
		graphs, or words.					
3.	Quantitative	Analyzing problems to extract and quantify essential features.					
	Reasoning Skills	Inductive and deductive reasoning.					

Table Caption 1. Modification indicator of algebraic thinking

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Instrument for this research were algebraic test paper and transcrip of interview which is completed of validation for specialist instructor from university and mathemathic teacher. The next steps to take a specimen of students who study carefully before it to found validity and reability for the instrument. The conclusion used triangulasi (Patton, 1999: 1193) until obtained a really valid data.

RESULTS AND DISCUSSION

Analyzed Test For Algebraic Thinking In Mathematic Problem Solving By Low Student Ability Based On Quantitative Reasoning Ability.

1. The first algebraic thinking test.

	a. 11.45000 10.46000 × 13000 = 2 2.165.000
Penyelesaian : C (Ate) +	(1003)
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Image 1. Test Result 1 By Subject GF

Р	:	Now see your answer for 1a. The question, how many apples were obtained if
		you have Rp. 45,000, And if on the paper was already knew the price of 1 apple
CE		was Rp. 5,000, What about your settlement?
GF		Um It's means 45000 divided by 5000, ma'am. Then the answer ??
Р	:	Look, why here (<i>pointed to the subject answer sheet</i>) 45000 multiplied by 13000 ??
GF	:	Hheheee Yes ma'am, I was still confused
Р	:	Next time I accurately your answer again
GF	:	Okay, ma'am, that means for number 1b must be 5000 multiplied by 13 apples, that right??
Р	:	Yes, absolutely. On 1a problem, the question was how many <i>n</i> apples gain? What
		the meaning of <i>n</i> on this problem ??
GF	:	Umm I didn't knew ma'am
Р	:	How many <i>n</i> apples were obtained in the problem meaning how many apples
		would the buyer gain. Could you understood ??
GF	:	Yes. I understood (nod subject head)
Р	:	Did you still remember to represent the function?
GF	:	Functions, relations, tables Umm
Р	:	It's not that!! Remember, we represented arrows diagram with the points on the
		lines, you know ??
GF	:	Umm (trying to recall memoriez)
Р	:	Okay, you know after we learned the set, comprehend of the function. We make
		as like as those circles. Did you remember??
GF	:	Umm Did you mean the arrow diagram, set sequential pairs and cartesius
-		diagram?
Р	:	Yes. Then, you could explain your solution to the number 1c problem?

Available online at Journal homepage: ejournal.<u>iainkerinci.ac.id/</u>index.php/edumatika Email: edumatika@iainkerinci.ac.id **GF** : Um (*smiling and shaking his head*) Image 2. Interview Transcrip Of Subject GF

Algebraic thinking test for number one showed, subject didn't capable to solved with suitable problem solving steps used function formula because subject didn't comprehend with the problem. The calculation which is subject appeared untrue. Subject didn't capable on clarify *n* symbol on problem solved and representation on arrow diagram and cartesius diagram which refer a relation between apple quantity and apple cost. Subject didn't wrote the solved on answer paper too. Beside that, interview transcipt showed subject didn't capable to comunicated a steps of problem solved. It was showed that subject didn't capable used deductive reasoning on clarify *n* symbol on problem and representation on arrow diagram and cartesius diagram for the first problem test. The result that *Quantitative Reasoning* subject on analyzing problems to extract and quantify essential features with deductive reasoning obtained "Less" category.

2. The second algebraic thinking on problem solving test.

	<u>Ditenza:</u> a Susunlah tobel mlatitugat b Sambarlah galpin funga h Ara haatilmah cartaeur b Sambarlah galpin funga h Minga 3 c kalpin bola lib Imendaput Janan Minga 3										
1	envel	esaian	1								
The Fruit	0 0	1 25	2 40	3	4 40	5 25	6]		
	= = F(J)			(0)" = 5" (0) = 5" (1) = 5" (1)	c ¹) ¹	R	=90 = 9	.3 -5 0-4		(3)	

Image 3. Test Result 2 By Subject GF

Р	:	Look for the question number 2. Did you know about the problem ??
GF	:	
		(while pointed on the answer sheet)
Р	:	What the problem for that number?
GF	:	That was ma'am (while showed the answer has been done on the answer sheet)
Р	:	Okay, now check your answers number 2a and 2b. It was correct or not ??
GF	:	(Shake his head)
Р	:	Now. Explain to ma'am, how you get this result? (while pointed to the subject's
		answer sheet)
GF	:	When I did on sheet, those was $h(t) = 30t - 5t^2$. And the question was valued h
		(3). So, the point 3 substitution on the t, then i did calculation $30.3 - 5 (3)^2$ until
		get the result is 45.
Р	:	Okay, where your graph function ??
GF	:	Not yet ma'am, I couldn,t explained
Р	:	It's okay, another time try to studied again. Later, based on your previous
		calculation of founded the value of the function (while pointed to the answer sheet
		of the subject). When the ball reach the highest bounce ?
GF	:	Ehmmm If I look for my calculation. It means, the highest ball bounce as far as
		45 meters, when it was substitution by 3 pointed ma'am
Р	:	Yes, thanks

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Image 4. Interview Transcript Of Subject GF

Algebraic thinking test for number two showed subject didn't capable to understood about the problem on paper. Subject didn't communicated about a steps for problem solved when subject interviewing. Subject try to make a function table with function calculate value. It was mean subject replaced value of t = 0 until t = 6 on function formula which is available on paper eventhough didn't make a graph for the last solved problem. Beside that, on interview transcript subject didn't verified to representation on graph clearly which is graph function of $h(t) = 30t - 5t^2$ could clarified to make a conclusion about highest bounce of the ball. It was showed subject didn't capable used inductive reasoning on conclude highest bounce of the ball from the grapich and function table. With the result that *Quantitative Reasoning* subject on analyzing problems to extract and quantify essential features with inductive reasoning obtained "Less" category.

CONCLUSION

Based on each percentage of achievement by algebraic thinking test and questionnaire with some descriptive achievement from the test, it could be concluded that algebraic thinking processed by low mathematic ability based on *quantitative reasoning* ability obtained Less category because subject didn't capable used deductive reasoning on clarify *n* symbol on problem solved and representation on arrow diagram and cartesius diagram for the first algebraic thinking test. So, the result that *Quantitative Reasoning* subject on analyzing problems to extract and quantify essential features with deductive reasoning obtained "Less" category. The second algebraic thinking test, subject didn't capable used inductive reasoning on concluded highest bounce of the ball from the graph and function table. So, the result that *Quantitative Reasoning* subject on analyzing problems to extract and quantify essential features with inductive reasoning obtained "Less" category. The percentage of algebraic thinking test for GF subject was 35.

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